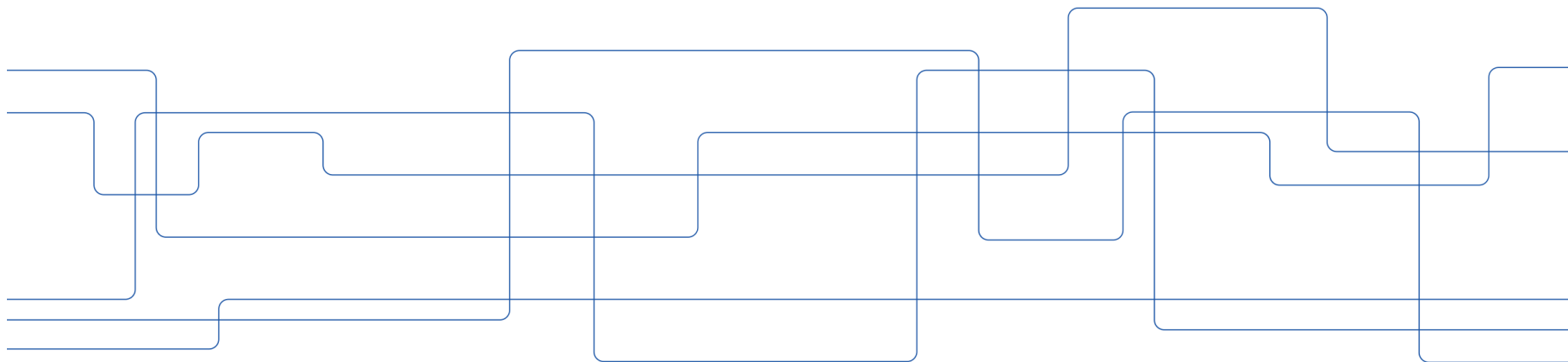




# Assembly line balancing

Fabio Marco Monetti

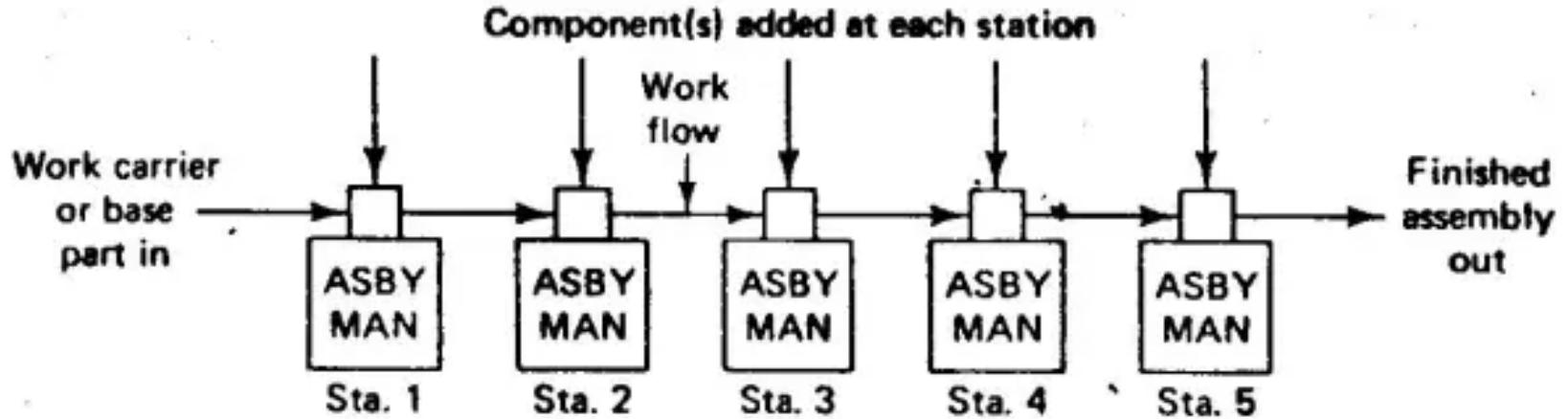




# Recap: assembly systems

1. Manual single-station assembly
  - Single workplace station → full assembly
  - Complex product, small quantities, extremely high variance
  - One or more workers
2. Manual assembly line
  - Multiple workstation → part of assembly/subassembly
  - Product passes along the line
  - One or more workers per station
  - Medium batch size, possible high variance
3. Automated assembly line
  - Automated methods for assembly
  - Less human workers as possible
  - High production rate, low variance

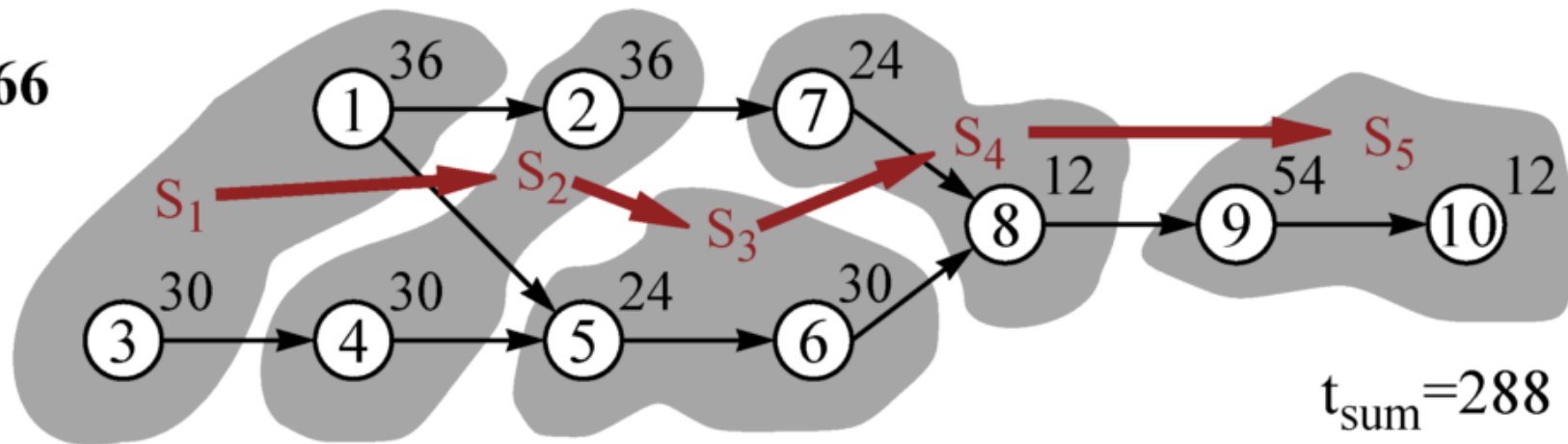
# Manual assembly lines



- Conveyor belt?
- Problems?
- Solutions?

# SALBP

$c = 66$





# SALBP

- Simple assembly line balancing problem
  - SALBP-F
  - SALBP-1
  - SALBP-2
  - SALBP-E
- Other assembly line balancing problem
  - ARALBP
  - SDALBP
  - SUALBSP
  - ASALBP...



# Line balancing problem

- Things to keep in mind:
  - List of parts
  - Connections
  - Assembly operations
  - Precedence constraints
  - Desired production rate
  - Manual/automatic assembly
  - Efficiency

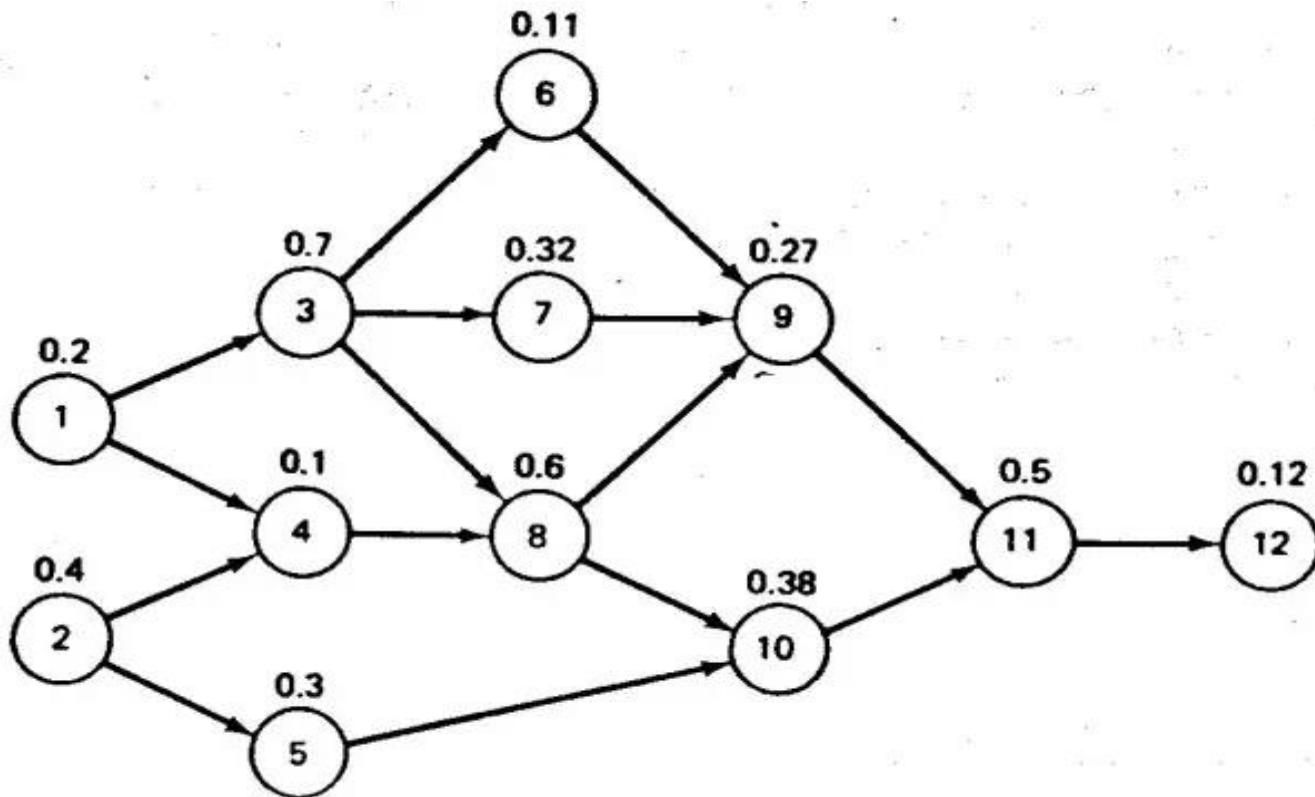
# Example

No.	Element description	$T_d$	Must be preceded by:
1	Place frame on workholder and clamp	0.2	—
2	Assemble plug, grommet to power cord	0.4	—
3	Assemble brackets to frame	0.7	1
4	Wire power cord to motor	0.1	1, 2
5	Wire power cord to switch	0.3	2
6	Assemble mechanism plate to bracket	0.11	3
7	Assemble blade to bracket	0.32	3
8	Assemble motor to brackets	0.6	3, 4
9	Align blade and attach to motor	0.27	6, 7, 8
10	Assemble switch to motor bracket	0.38	5, 8
11	Attach cover, inspect, and test	0.5	9, 10
12	Place in tote pan for packing	0.12	11

$$T_{WC} = \sum_{j=1}^{n_r} T_{ej}$$

$$T_c \leq \frac{E}{R_p}$$

# Precedence constraints







# Other constraints

- Zoning constraint
  - Positive
  - Negative
- Position constraint

(Not to be considered in course/examples/test)

→ But important to consider for the project!



# Methods for line balancing

1. Largest-candidate rule
2. Kilbridge and Wester's method
3. Ranked positional weights method

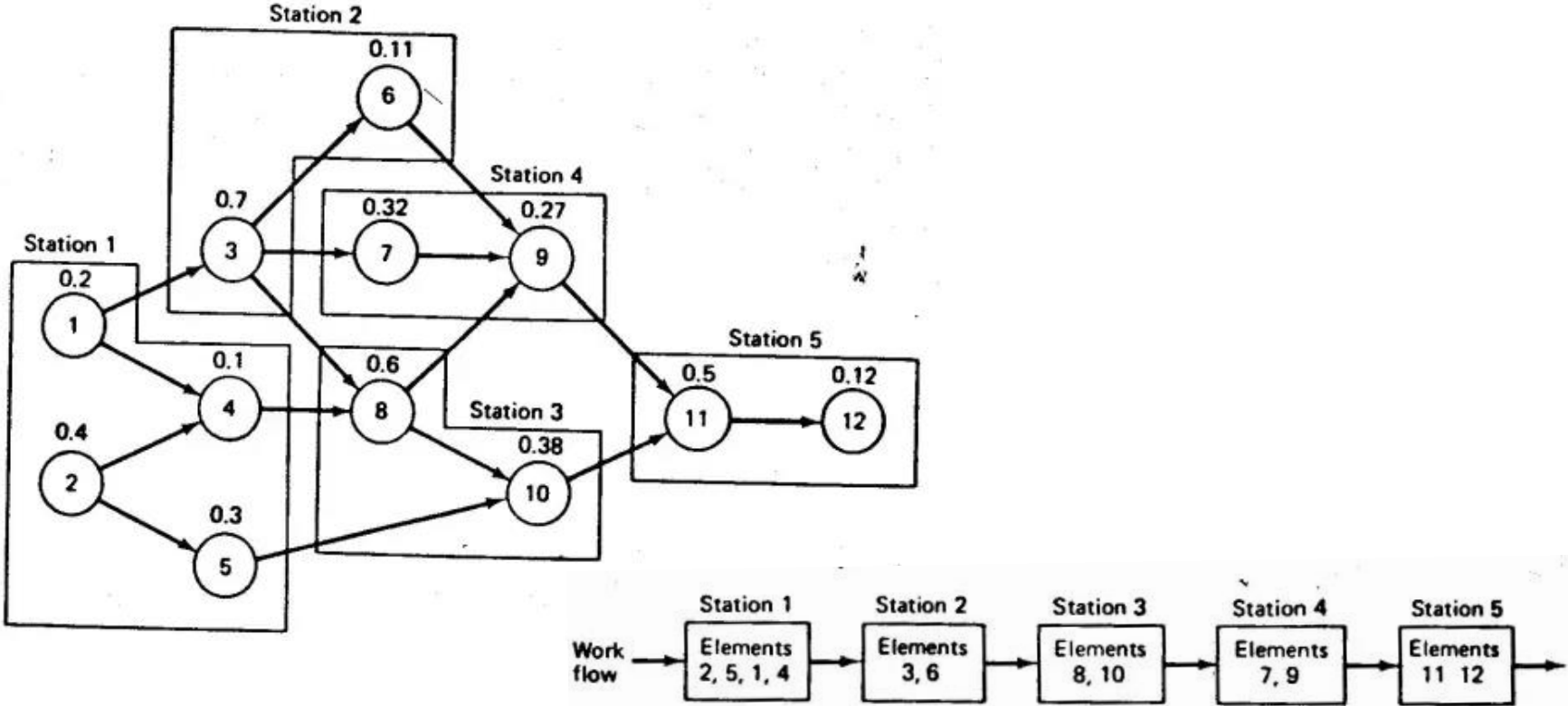
# Largest-candidate rule (LCR)

$$T_c = 1 \text{ min}, E = 1$$

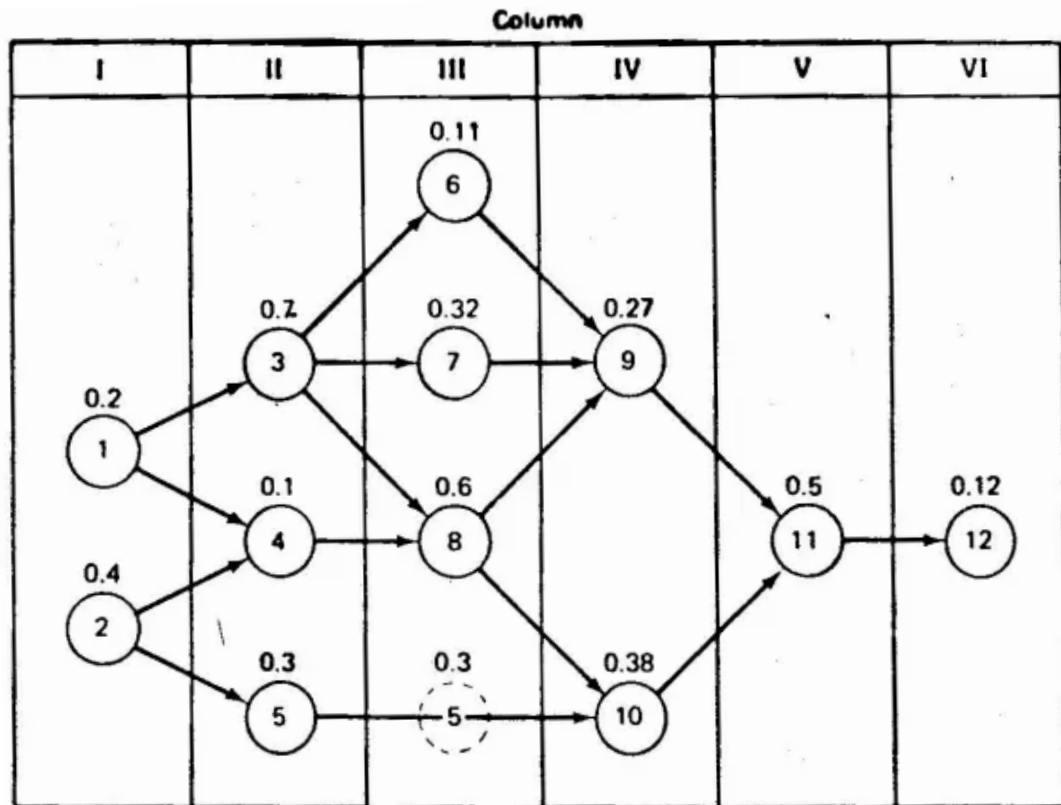
<i>Work element</i>	$T_e$	<i>Immediate predecessors</i>
3	0.7	1
8	0.6	3, 4
11	0.5	9, 10
2	0.4	—
10	0.38	5, 8
7	0.32	3
5	0.3	2
9	0.27	6, 7, 8
1	0.2	—
12	0.12	11
6	0.11	3
4	0.1	1, 2

<i>Station</i>	<i>Element</i>	$T_e$	$\Sigma T_e$ at station
1	2	0.4	1.00
	5	0.3	
	1	0.2	
	4	0.1	
2	3	0.7	0.81
	6	0.11	
3	8	0.6	0.98
	10	0.38	
4	7	0.32	0.59
	9	0.27	
5	11	0.5	0.62
	12	0.11	

# Solution



# Kilbridge and Wester's (K&W)



Work element	Column	$T_e$	Sum of column $T_e$ s
1	I	0.2	
2	I	0.4	0.6
3	II	0.7	
4	II	0.1	
5	II,III	0.3	1.1
6	III	0.11	
7	III	0.32	
8	III	0.6	1.03
9	IV	0.27	
10	IV	0.38	0.65
11	V	0.5	0.5
12	VI	0.12	0.12

# Solution

<i>Station</i>	<i>Element</i>	$T_r$	$\Sigma T_r$ at station
1	1	0.2	
	2	0.4	
	4	0.1	
	5	0.3	1.00
2	3	0.7	
	6	0.11	0.81
3	7	0.32	
	8	0.6	0.92
4	9	0.27	
	10	0.38	0.65
5	11	0.5	
	12	0.12	0.62

# Ranked positional weights (RPW)

<i>Element</i>	<i>RPW</i>	<i>T<sub>e</sub></i>	<i>Immediate predecessors</i>
1	3.30	0.2	—
3	3.00	0.7	1
2	2.67	0.4	—
4	1.97	0.1	1,2
8	1.87	0.6	3,4
5	1.30	0.3	2
7	1.21	0.32	3
6	1.00	0.11	3
10	1.00	0.38	5,8
9	0.89	0.27	6,7,8
11	0.62	0.5	9,10
12	0.12	0.12	11

# Solution

<i>Station</i>	<i>Element</i>	$T_e$	$\Sigma T_e$ at station
1	1	0.2	0.9
	3	0.7	
2	2	0.4	0.91
	4	0.1	
	5	0.3	
	6	0.11	
3	8	0.6	0.92
	7	0.32	
4	10	0.38	0.65
	9	0.27	
5	11	0.5	0.62
	12	0.12	





# Model variations

1. Single-model line
2. Batch-model line
3. Mixed-model line



# Computerized line balancing methods

1. COMSOAL
2. CALB
3. ALPACA

(Not investigated in this course)