

TASK 1

In a factory, the assembly line uses a conveyor belt driven by a **synchronous electric motor**. The motor is 3-phase, 30 kW , operates at a frequency of 50 Hz and a voltage of 400 V . The power factor of the motor is 0.8 , and the synchronous speed of the motor is 1800 rpm .

Determine:

- a) Synchronous reactance X_S and rated motor current I_N
- b) The torque M developed by the motor
- c) Motor efficiency η

Data:

$$P = 30\text{ kW}$$

$$U = 400\text{ V}$$

$$f = 50\text{ Hz}$$

$$v = 1800\text{ rpm}$$

$$\cos\varphi = 0.8$$

$$X_S, I_N = ?$$

$$M, \eta = ?$$

TASK 2

The water pump is driven by a 3-phase, 50 Hz, 400 V, 15 kW synchronous motor. The efficiency of the motor is 92% and the power factor is 0.9. The motor speed is 1500 rpm.

- What current does the motor consume?
- Determine the real, reactive and apparent power of the motor.
- Calculate the value of the capacitive element that will correct the power factor of the motor to 0.95.

Data:

$$P = 15 \text{ kW}$$

$$U = 400 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$v = 1600 \text{ rpm}$$

$$\cos \varphi = 0.9$$

$$\eta = 92\%$$

$$I_L = ?$$

$$P_T, P_R, P_A = ?$$

$$C \text{ for } \cos \varphi = 0.95$$

TASK 3

We use a 3-phase 1.5 MW synchronous motor operating at a frequency of 50 Hz and a voltage of 4.16 kV in the paper mill to drive loads with high inertia. The power factor is 0.9, and the synchronous speed is 1200 rpm. For smooth start-up and speed control, the motor is equipped with a variable frequency drive (VFD). The synchronous reactance of the motor X_S is 3.0 Ω per phase.

Determine:

- rated current I_N and apparent motor power P_A ,
- motor torque M at full load,
- the internally generated voltage U_a on each phase when the connection voltage U is equal to 4.16 kV,
- the phase angle between the internally generated voltage and the connection voltage.

Data:

$$P = 1.5 \text{ MW}$$

$$U = 4.16 \text{ kV}$$

$$f = 50 \text{ Hz}$$

$$X_S = 3 \text{ } \Omega \text{ per phase}$$

$$v = 1200 \text{ rpm}$$

$$\cos\varphi = 0.9$$

$$I_N, P_A = ?$$

$$M = ?$$

$$U_a = ?$$

$$\varphi = ?$$

TASK 4

The electric vehicle uses a 3-phase, 400 V, 150 kW synchronous motor with a power factor of 0.95 for propulsion. The motor is powered by a 600 V DC battery and a 3-phase variable frequency drive (VFD) to control the motor speed. The synchronous reactance of the X_S motor is 1.0 Ω per phase, and the synchronous speed is 10.000 rpm.

- Calculate the nominal current I_N and the apparent motor power P_A .
- Determine the torque T developed by the motor at full load.
- The internally generated voltage U_a on each phase when the connection voltage U is equal to 400 V.
- Find the phase angle between the internally generated voltage and the terminal voltage when the motor is operating at a power factor of 0.95.

Data:

$$P = 150 \text{ kW}$$

$$U = 400 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$X_S = 1 \text{ } \Omega \text{ per phase}$$

$$v = 10000 \text{ rpm}$$

$$\cos \varphi = 0.95$$

$$I_N, P_A = ?$$

$$M = ?$$

$$U_a = ?$$

$$\varphi = ?$$

TASK 5

We use a single-phase 230 V, 0.75 kW induction motor to drive the fan. The motor has an efficiency of 85% and a power factor of 0.82. Slip at full load is 5%. The synchronous speed is 1800 rpm.

- Calculate the rotor speed at full load.
- Determine the current drawn by the motor at full load.
- Calculate the torque M developed by the motor at full load.

Data:

$$U = 230 \text{ V}$$

$$P = 0.75 \text{ kW}$$

$$\text{slip} = 5 \%$$

$$v = 1800 \text{ rpm}$$

$$\cos\varphi = 0.82$$

$$\eta = 85\%$$

$$v_R = ?$$

$$I = ?$$

$$M = ?$$

TASK 6

A 3-phase 60 Hz, 480 V, 20 HP induction motor drives the water pump. The motor has an efficiency of 90% and a power factor of 0.87. Slip at full load is 4%. The synchronous speed is 1800 rpm.

- Calculate the rotor speed at full load.
- Determine the current drawn by the motor at full load.
- Calculate the torque M developed by the motor at full load.

Data:

$$U = 480 \text{ V}$$

$$P = 20 \text{ HP}$$

$$\text{slip} = 4\%$$

$$v = 1800 \text{ rpm}$$

$$\cos\varphi = 0,87$$

$$\eta = 90\%$$

$$v_R = ?$$

$$I = ?$$

$$M = ?$$

TASK 7

We use a 50 Hz, 415 V, 22 kW 3-phase induction motor to drive the conveyor system. The motor has a full load efficiency of 90% and a power factor of 0.86. The engine is started with a **direct-on-line starter (DOL)**. Slip at full load is 3%.

- Calculate the synchronous speed and rotor speed at full load.
- Determine the torque M developed by the motor at full load.
- Calculate the starting current I_{ST} of the motor when using a DOL starter.

Data:

$$U = 415 \text{ V}$$

$$P = 22 \text{ kW}$$

$$f = 50 \text{ Hz}$$

$$\text{slip} = 3 \%$$

$$\cos\varphi = 0.86$$

$$\eta = 90\%$$

$$v_S, v_R = ?$$

$$M = ?$$

$$I_{ST} = ?$$

TASK 8

The crane uses a 3-phase, 60 Hz, 480 V, 75 kW **wound rotor induction motor** for its lifting mechanism. The motor has a full load efficiency of 92% and a power factor of 0.88. Slip at full load is 6%. The stator resistance R_s of the motor and the rotor resistance R_r are 0.2 Ω per phase and 0.15 Ω per phase, respectively. Stator reactance X_s and rotor reactance X_r are 1.8 Ω per phase and 1.5 Ω per phase respectively.

- Calculate the rotor speed at full load.
- Determine the torque M developed by the motor at full load.
- Calculate the line current I_L consumed by the motor at full load.
- Find the starting torque T_{ST} of the motor as a percentage of the full load torque T .

Data:

$$U = 480 \text{ V}$$

$$P = 75 \text{ kW}$$

$$f = 60 \text{ Hz}$$

$$\text{slip} = 6 \%$$

$$\cos\varphi = 0.88$$

$$\eta = 92\%$$

$$R_s = 0.2 \text{ } \Omega \text{ per phase}$$

$$R_r = 0.15 \text{ } \Omega \text{ per phase}$$

$$X_s = 1.8 \text{ } \Omega \text{ per phase}$$

$$X_r = 1.5 \text{ } \Omega \text{ per phase}$$

$$v_R = ?$$

$$M = ?$$

$$I_L = ?$$

$$T_{ST} = ?$$

TASK 9

A 3-phase, 60 Hz, 480 V, 100 HP squirrel-cage induction motor drives a large industrial fan. We control the motor by a variable frequency drive (VFD) that allows varying the speed of the motor. The motor has a full load efficiency of 92% and a power factor of 0.9. The VFD is set to operate the motor at 75% of its synchronous speed.

- Calculate the synchronous speed and rotor speed.
- Determine the torque M developed by the motor.
- Calculate the line current I_L drawn by the motor.

Data:

$$U = 480 \text{ V}$$

$$P = 100 \text{ HP}$$

$$f = 60 \text{ Hz}$$

$$\cos\varphi = 0.9$$

$$\eta = 92\%$$

$$v_S, v_R = ?$$

$$M = ?$$

$$I_L = ?$$

TASK 10

We use a three-phase, 50 Hz, 415 V, 30 kW **double-cage induction motor** in an application that requires high starting torque. The motor has an efficiency of 90% and a power factor of 0.85. Slip at full load is 4%. The outer cage has a higher resistance and lower reactance than the inner cage. The synchronous speed is 1500 rpm.

- Calculate the rotor speed at full load.
- Determine the torque M developed by the motor at full load.
- Calculate the line current I_L consumed by the motor at full load.
- Explain how a double cage induction motor achieves a higher starting torque compared to a conventional single cage induction motor.

Data:

$$U = 415 \text{ V}$$

$$P = 30 \text{ kW}$$

$$f = 50 \text{ Hz}$$

$$\text{slip} = 4 \%$$

$$\cos\varphi = 0.85$$

$$\eta = 90\%$$

$$v = 1500 \frac{\text{revs}}{\text{min}}$$

$$v_R = ?$$

$$M = ?$$

$$I_L = ?$$

$$T_Z = ?$$